## Kansas City Area Teachers of Mathematics 2011 KCATM Math Competition

## GEOMETRY AND MEASUREMENT TEST GRADE 6

## INSTRUCTIONS

- Do not open this booklet until instructed to do so.
- Time limit: 20 minutes
- You may use calculators.
- Mark your answer on the Scantron sheet by FILLING in the oval.
- You may not use rulers, protractors, or other measurement devices on this test.
- Letter " $E$ " is "None of the above". It is a correct answer for some of the problems.
- Use the $\pi$ key or 3.14159 on your calculator.
- The pictures in the figures are "not-to-scale."

1. Which angle values shown in Figure $\mathbf{1}$ show congruent angles?
A.

B.

C.

D.

E. None of the above

Figure 1
2. If you continue to add sides to a convex polygon, what figure does the polygon get closer to looking like?
A. a dodecagon
B. an octagon
C. a hexagon
D. a circle
E. None of the above
3. Point T is the midpoint of $\overline{M H}$, and A is the midpoint of $\overline{M T}$ in Figure 2. What is the coordinate of pt. M when AT = 3 and H is " 0 "?

Figure 2

A. -3
B. -6
C. -9
D. -12
E. None of the above
4. Which name correctly describes the information shown in Figure 3?
A. Acute $\angle J A M$
B. $\angle A M J$
C. Right $\angle \mathrm{MAJ}$
D. Obtuse $\angle \mathrm{JMA}$
E. None of the above

5. Which statement is NOT necessarily true about Figure 4?
A. Opposite rays $\overrightarrow{O H}$ and $\overrightarrow{O T}$
B. O is between points H and T


Figure 4
C. O is the midpoint of $\overrightarrow{H T}$
D. $\angle \mathrm{HOT}$ is a straight angle
E. None of the above
6. Name the geometric shape in Figure 5.
A. tetrahedron
B. cone
C cylinder
D. pyramid
E. None of the above


Figure 5

For questions \#7-9, refer to the coordinate plane shown in Figure 6.
7. Name the coordinates of point has the coordinates of point M.
A. $(1,-3)$
B. $(3,-1)$
C. $(-3,1)$
D. $(-1,3)$
E. None of the above
8. If triangle MKL is reflected over the $x$ axis, what would be the point of reflection for point K ?
A. $(-2,-5)$
B. $(2,5)$
C. $(-2,5)$
D. $(2,-5)$
E. None of the above


Figure 6
9. What is the area of $\triangle M K L$ ?
A. 6 sq. units
B. 7 sq. units
C. 8 sq. units
D. 9 sq. units
E. None of the above

For questions \#10.-11., refer to the Figure 7. $\overline{\mathrm{AB}}$ is 13 cm long. Point $B$ is the center of the circle.
10. What is the length $D E$ ?
A. 10 cm
B. 20 cm
C. 27 cm
D. 50 cm
E. None of the above


Figure 7
11. To the nearest one-tenth of a cm, what is the circumference of circle B?
A. 530.9 cm
B. 81.7 cm
C. 35.3 cm
D. 20.4 cm
E. None of the above
12. A Kindle book reader has dimensions of 4.75 " by 7.5 ". If the viewing screen is 3 " by 5 ", what is the area that is does not show printed material? (Figure 8) Round to the nearest hundredth.
A. $35.63 \mathrm{in}^{2}$
B. $20.63 \mathrm{in}^{2}$
C. $15.00 \mathrm{in}^{2}$
D. $20.35 \mathrm{in}^{2}$
E. None of the above


Figure 8
13. What is the degree of rotational symmetry in Figure 9 ?

Figure 9
A. $30^{\circ}$
B. $45^{\circ}$
C. $60^{\circ}$
D. $90^{\circ}$
E. None of the above

14. The lama tessellation in Figure 10 shows what type of transformation?

A. reflection
B. translation
C. dilation
D. rotation
E. None of the above

Figure 10
15. Which triangle has the largest area in Figure 11?


D

Base $=9$
E. None of the above

Figure 11
16. Which statement is ALWAYS true?
A. A polygon is always a quadrilateral.
B. A square is always a parallelogram.
C. A rhombus is always a square.
D. A trapezoid is always a parallelogram.
E. All statements are always true.
17. According to the highway sign in Figure 12, 10 miles is equal to 16 kilometers. If the sign would have said Bowling Green: 30 miles, how
 many kilometers would the sign say?
A. 32 km
B. 48 km
C. 64 km
D. 16 km
E. None of the above

Figure 12
18. How many centimeters are in 2.8 meters?
A. 2.8 cm
B. 28 cm
C. 28 cm
D. 280
E. None of the above
19. Seventy-five kilometers is how many meters?
A. 75 m
B. 750 m
C. 7,500
D. $75,000 \mathrm{~km}$
E. None of the above
20. You have invited your friends to come over to play games on your new Kinect for the Xbox 360 . When you get home from school at 3:52, your mom asks you to do chores. Your friends are coming over at 5:10. How much time do you have to help your mom before they arrive?
A. 1 hr .18 min .
B. 1 hr .8 min .
C. 2 hr .18 min .
D. 2 hr .8 min .
E. None of the above
21. You have a cell phone plan that lets you talk for 400 minutes per month free during the prime rate time. If you talk to your friends for the following amounts during the prime rate time, how many minutes do you still have left for the month?

$$
30 \text { min.; } 1 \text { hr.; } 45 \text { min.; } 1 \text { 1⁄2 hour }
$$

A. 55 min .
B. 175 min .
C. 255 min .
D. 120 min .
E. None of the above
22. HDTVs are longer horizontally that old TVs. Find the width of the 32" TV in Figure 13 (Round your answer to the nearest integer).

Figure 13

A. 28 in .
B. 27 in.
C. 26 in.
D. 25 in .
E. None of the above
23. Use the geoboard in Figure 14. The distance between each dot on the geoboard is $1 \mathbf{c m}$. Find the area of the composite shape made up of the four triangles and one square.


Figure 14
A. 5 sq. units
B. 6 sq. units
C. 8 sq. units
D. 10 sq. units
E. None of the above
24. Determine the length of the line segment represented by $x$, given 2 parallel lines cut by the two transversals
A. 18
B. 3
C. 27
D. 36
E. None of the above


Figure 15
25. Determine the length CD given similar triangles in Figure 16.
A. 5
B. 8
C. 10
D. 12
E. None of the above


Figure 16
26. Find the area of the trapezoid in Figure 17. $A=1 / 2 h\left(b_{1}+b_{2}\right)$
A. $130 \mathrm{sq} . \mathrm{cm}$
B. $208 \mathrm{sq} . \mathrm{cm}$
C. $156 \mathrm{sq} . \mathrm{cm}$
D. 494 sq. cm
E. None of the above

27. Determine the amount of wax (to the nearest cubic inch) in a candle that is 3 " in diameter and stands $53 / 4$ " tall as in Figure 18.

Formula for Volume of a Cylinder: $V=\pi r^{2} h$
A. $163 \mathrm{in}^{3}$
B. $41 \mathrm{in}^{3}$
C. $94 \mathrm{in}^{3}$
D. $47 \mathrm{in}^{3}$
E. None of the above

Figure 18
28. How many faces does an octagonal prism have? (See Figure 19)
A. 2
B. 5
C. 8
D. 10
E. None of the above


Figure 19
29. How many sides does a decagon have?
A. 7
B. 10
C. 12
D. 9
E. None of the above.
30. Figure $\mathbf{2 0}$ is a tetrahedron. What other name can it be called?

Figure 20
A. Triangular prism
B. Triangular pyramid
C. Square pyramid
D. Triangle
E. None of the above
31. Determine the value of the vertex angle in the obtuse isosceles triangle in Figure 21.


Figure 21
32. Find the value of the acute angle in Figure 22.

A. $19^{\circ}$
B. $148^{\circ}$
C. $32^{\circ}$
D. $38^{\circ}$
E. None of the above
33. Find the measure of $\angle B$ in the isosceles trapezoid ABCD in Figure 23.


Figure 23
A. $123^{\circ}$
B. $117^{\circ}$
C. $63^{\circ}$
D. $127^{\circ}$
E. None of the above
34. Find the surface area of the earth if the radius of earth is approximately 3960 miles. See Figure 24. Surface Area of a Sphere: $A=4 \pi r^{2}$
A. $11,581,167$ sq. miles
B. 49,762 sq. miles
C. 99,525 sq. miles.
D. 197,060,797 sq. miles
E. None of the above
35. How many marbles would be in the triangular pyramid stack Figure 25?

Figure 25
A. 24
B. 21
C. 20
D. 16
E. None of the above
36. Find the area of the T in Figure 26.

Figure 26

A. $29 \mathrm{~cm}^{2} \quad$ B. $36 \mathrm{~cm}^{2}$
C. $33 \mathrm{~cm}^{2}$
D. $42 \mathrm{~cm}^{2}$
E. None of the above
37. What is the geometric probability of landing on square (\#5) in the square grid of tangram pieces in Figure 27?
A. $1 / 4$
B. $1 / 3$
C. $1 / 6$
D. $1 / 8$
E. None of the above

Figure 27

38. Find the perimeter of the composite figure in Figure 28?

39. How many edges does a cube have?
A. 6
B. 8
C. 10
D. 12
E. None of the above
40. President Dwight D. Eisenhower signed a decree on August 21, 1959 stating the correct proportions of each part of the US Flag. Find the area of the canton (blue section) on an indoor flag measuring 3' by 5'. The length of the canton is $2 / 5$ the length of the flag and its width goes to the bottom of the $4^{\text {th }}$ red stripe? See Figure 29.

A. 3.23 sq. feet
B. 2.77 sq. feet
C. 1.85 sq. feet
D. 3.75 sq. feet
E. None of the above

